

# Predicting Regional Food Production Under Climate Uncertainty with Probabilistic Deep Networks

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## Abstract

Regional food production forecasting under climate uncertainty represents one of the most pressing challenges at the intersection of environmental science and computational intelligence. Traditional deterministic models often fail to capture the compounding uncertainties arising from volatile precipitation regimes, temperature anomalies, and shifting growing seasons. This study proposes a probabilistic deep network (PDN) framework integrating Monte Carlo dropout with a hybrid recurrent encoder and a temporal attention mechanism to generate calibrated uncertainty bounds for multi-crop yield prediction across heterogeneous agricultural regions. The model is trained on a 35-year retrospective dataset covering six major crop types across 480 administrative units in East Asia and Sub-Saharan Africa, augmented with ERA5 reanalysis climate variables and MODIS-derived vegetation indices. Experimental results demonstrate that the proposed PDN achieves a root mean square error of 0.31 tonnes per hectare and a continuous ranked probability score of 0.18, outperforming baseline recurrent networks and ensemble regression methods by margins of 14% and 22%, respectively. Uncertainty quantification calibration evaluated through prediction interval coverage probability confirms that 90% prediction intervals contain the true yield in 88.4% of test instances, validating the practical utility of the probabilistic framework for climate adaptation planning and food security governance.

## Keywords

probabilistic deep network, crop yield prediction, climate uncertainty, recurrent neural network, uncertainty quantification, Monte Carlo dropout, agricultural forecasting

## 1. Introduction

The stability of regional food systems increasingly depends on the capacity to forecast agricultural output with sufficient accuracy and sufficient temporal lead time to allow adaptive responses by governments, supply chains, and farming communities. Yet the growing unpredictability of climatic drivers—amplified by anthropogenic climate change—has fundamentally undermined the reliability of conventional forecasting methods that assume stationary relationships between weather patterns and crop yields. The Intergovernmental Panel on Climate Change Sixth Assessment Report documented with high confidence that even 1.5°C of global warming above pre-industrial levels will generate detectable yield reductions in major staple crops across tropical and subtropical regions, with the compounding effects of drought frequency and heat stress creating nonlinear yield responses that conventional statistical frameworks are ill-equipped to model [1]. Against this backdrop, the development of data-driven forecasting systems capable of simultaneously generating accurate predictions and quantifying associated uncertainty has emerged as a

scientific and policy priority of considerable urgency. The rapid maturation of machine learning has offered partial solutions to this challenge, and the research community has responded with a growing body of work linking climatic data to agronomic outcomes through increasingly sophisticated architectures. Rolnick et al. provided a landmark synthesis of the potential for machine learning across the climate science domain, identifying food system forecasting as a high-leverage application area where algorithmic advances could translate directly into actionable decision support [2]. Central to the value proposition of such systems is the notion that predictions must be not only accurate in expectation but also accompanied by well-calibrated expressions of uncertainty—an ideal that most deployed systems fall far short of realizing. This gap between the ideal of calibrated probabilistic prediction and the reality of deterministic operational forecasting models is the organizing problem motivating the present study. Deep neural networks (DNNs) have demonstrated remarkable capacity to capture the nonlinear, temporally lagged relationships between climatic inputs and agronomic outcomes. Among architectures applied to agricultural time series, recurrent neural network (RNN) variants—particularly long short-term memory (LSTM) networks—have proven especially well-suited to the sequential nature of crop growth dynamics, learning dependencies across a full growing season in ways that static regression models cannot. Khaki and Wang demonstrated through systematic evaluation that deep neural network architectures applied to multi-year crop sequence data outperform conventional machine learning baselines by substantial margins when training data span diverse agroecological zones, establishing a foundational empirical case for the deployment of deep recurrent architectures in regional yield prediction [3]. Despite these architectural strengths, the majority of existing deep learning applications in agricultural forecasting produce point predictions that provide no information about the confidence or reliability of individual forecasts—a limitation with direct consequences for risk-sensitive decision-making. A policymaker designing emergency grain reserves based on a predicted 20% shortfall in regional wheat production faces fundamentally different decisions depending on whether that prediction carries a narrow or a wide confidence interval. The failure to communicate and quantify uncertainty is therefore not merely a technical shortcoming but a critical impediment to translating predictive capabilities into evidence-based governance. Leng and Hall identified this dimension of agricultural forecasting as a persistent vulnerability in existing early warning architectures, demonstrating that yield sensitivity to drought is systematically underestimated when deterministic model outputs are fed directly into policy decision frameworks without uncertainty propagation [4]. The quantification of predictive uncertainty in DNNs has itself become a substantial research frontier, variously addressed through Bayesian neural networks, Monte Carlo (MC) dropout inference, deep ensembles, and conformal prediction methods. Abdar et al. provided a comprehensive survey distinguishing between methods that approximate full Bayesian inference, methods based on ensemble diversity, and methods that treat uncertainty quantification (UQ) as a post-hoc calibration problem, concluding that no single method universally dominates and that the optimal choice depends critically on application domain and computational constraints [5]. For agricultural applications specifically, where training data may be spatially heterogeneous and temporally limited, the choice of UQ method interacts non-trivially with model architecture in ways that demand careful empirical investigation. Ovadia et al. conducted a rigorous empirical comparison of major UQ methods under dataset shift conditions and demonstrated that distributional output training combined with inference-time dropout provides better-calibrated uncertainty than either approach in isolation, particularly in the moderate distributional shift conditions characteristic of cross-regional agricultural evaluation [6]. Climate uncertainty in food production forecasting arises from at least three distinct sources: intrinsic aleatoric uncertainty arising from irreducible stochasticity in precipitation and pest

pressure; parameter uncertainty stemming from limited observational records; and structural uncertainty arising from the choice of model architecture and the translation of general circulation model outputs to regional scales. Rasp et al. established through the WeatherBench benchmark that deep learning models can produce skillful medium-range forecasts of the temperature and precipitation variables most relevant to crop growth modeling, confirming the feasibility of using reanalysis and forecast products as PDN inputs [7]. This study introduces a PDN designed specifically to address multi-source uncertainty in regional food production prediction. By deploying MC dropout during inference, the model generates a posterior predictive distribution over yield outcomes rather than a single estimate, enabling the construction of credible intervals at any desired coverage level. The present work aligns with the emerging consensus in Earth system science, articulated by Reichstein et al., that hybrid models combining temporal sequence learning with learned spatial representations offer the most promising route to physically interpretable predictions that generalize robustly beyond the training distribution [8]. Beyond its empirical contributions, this work advances the discussion of how probabilistic deep learning outputs can be integrated into regional food security early warning systems, a topic that has received increasing attention from both the climate modeling community and the food policy literature concerned with extreme shortfall risks [9].

## 2. Literature Review

The application of machine learning to crop yield prediction has a history spanning several decades, but the rapid maturation of deep learning has fundamentally reshaped the methodological landscape. Systematic reviews have documented the broad empirical evidence that deep learning architectures consistently outperform conventional regression methods, random forests, and support vector machines in yield prediction tasks when sufficient training data are available. Van Klompenburg et al. conducted a comprehensive literature synthesis covering 50 primary studies and concluded that convolutional and recurrent neural network approaches dominate in terms of prediction accuracy when multi-temporal meteorological sequences are provided as inputs, largely because of their architectural capacity to model the temporal dependencies intrinsic to crop physiology [10]. The performance advantages are most pronounced in environments with high inter-annual climate variability, precisely the conditions under which reliable forecasting is most consequential for food security planning. Nevavuori et al. applied deep convolutional architectures to hyperspectral imagery from unmanned aerial vehicle platforms, demonstrating that spatial patterns in crop canopy structure captured by convolutional filters could improve yield estimation precision relative to traditional spectral indices, with  $R^2$  values exceeding 0.85 for barley and wheat in Finnish experimental plots [11]. Building on similar principles, Oikonomidis et al. examined the combination of convolutional and recurrent layers in hybrid architectures explicitly designed to process both spatial satellite imagery and temporal meteorological sequences, finding consistent accuracy improvements over single-modality approaches across diverse agroecological zones [12]. These studies collectively established that deep learning offers a scalable pathway to agronomic forecasting architecturally flexible enough to accommodate the diversity of input data types available in modern agricultural monitoring systems, and their findings directly inform the multi-stream feature integration strategy adopted in the present PDN design. The near-exclusive focus on point prediction accuracy in early agricultural deep learning work left a critical gap that subsequent research has begun to address systematically. Shahhosseini et al. analyzed machine learning performance for maize yield forecasting across Illinois, demonstrating that models incorporating environmental variable uncertainty significantly outperformed

deterministic counterparts during anomalous climate years, even when their mean accuracy was similar under normal conditions [13]. This result underscored the operational value of uncertainty-aware forecasting for food security applications, where the most consequential events are precisely those that deviate from historical norms. Li et al. arrived at complementary conclusions through a systematic analysis of statistical transparency in crop yield prediction, arguing that readable uncertainty decomposition—distinguishing climate-driven variance from management-related variance—is essential for the agronomic utility of any prediction system [14]. Together, these studies establish that the evaluation of probabilistic agricultural models must extend beyond mean prediction accuracy to encompass calibration quality, sharpness, and the practical interpretability of uncertainty outputs for end users. The parallel literature on uncertainty quantification in deep learning has meanwhile been developing principled frameworks for measuring and communicating predictive confidence in ways directly applicable to agricultural forecasting contexts. A particularly influential contribution from Schwalbert et al. demonstrated that machine learning models applied to satellite-derived vegetation indicators could produce calibrated county-level soybean yield forecasts across Brazil several months before harvest, with the combination of phenological features and meteorological anomaly indices reducing forecast uncertainty by 31% relative to univariate meteorological baselines [15]. Their analysis implicitly identified a trade-off between aleatoric and epistemic uncertainty that has since been more explicitly theorized: adding informative features reduces irreducible data uncertainty but may increase model uncertainty if the added features introduce distribution shift risk in future operational deployment. Cheng et al. provided an empirically grounded discussion of how MODIS time series products can be integrated into agricultural yield estimation pipelines in ways that minimize epistemic uncertainty arising from sensor data gaps and temporal compositing artifacts, offering practical guidance directly relevant to the remote sensing input stream used in the present study [16]. The development of neural network ensemble methods for weather and climate forecasting provided further methodological foundations relevant to the present framework. Scher and Messori demonstrated that ensembles of neural network-based weather forecast models produce probabilistic outputs that are competitive with physics-based ensemble systems at substantially lower computational cost, offering a practical pathway toward integrating data-driven uncertainty quantification into operational Earth system monitoring pipelines [17]. Yang et al. extended this line of inquiry by integrating LSTM-based temporal encoders with multi-head attention layers explicitly designed to focus on agronomically critical sub-periods of the growing season, achieving significant accuracy improvements for multi-crop, multi-region forecasting tasks using combined satellite and reanalysis inputs [18]. The attention mechanism introduced in their framework demonstrated that learned temporal weighting of growing-season inputs produces agronomically meaningful interpretations that align with expert knowledge of sensitive developmental periods, a finding that directly motivates the inclusion of a temporal self-attention component in the present PDN architecture. The broader case for deep learning in Earth system science was articulated by Eyring et al., who argued that rigorous model evaluation frameworks are essential for ensuring that data-driven predictions generalize reliably across the range of climate states encountered in operational deployment, rather than simply fitting historical patterns present in training data [19]. Shahhosseini et al. demonstrated in a complementary study that ensemble combinations of machine learning models trained on different feature subsets could reduce the variance of yield forecasts while improving mean accuracy relative to individual models, providing an ensemble-based uncertainty quantification baseline against which single-model probabilistic approaches can be benchmarked [20]. Peng et al. made a parallel argument in advocating for multiscale hybrid frameworks that leverage process-based knowledge to constrain data-driven learning at the regional scale, establishing

that the complementarity of mechanistic and data-driven models is particularly pronounced in physically heterogeneous environments where observation networks are sparse [21]. The food security policy dimension of probabilistic agricultural forecasting has been explicitly addressed in recent high-profile institutional analyses. The Food and Agriculture Organization of the United Nations has consistently identified forecast uncertainty as a barrier to effective early warning system design, particularly in low-income countries where government response windows are short and reserve margins are thin [22]. Lobell and Di Tommaso argued that the current generation of crop models—both process-based and data-driven—systematically underestimates the probability of extreme yield shortfalls because they are evaluated primarily on mean prediction accuracy rather than distributional coverage metrics [23]. Their argument implies that a shift toward probabilistic evaluation metrics, including the continuous ranked probability score and calibration reliability diagrams, is essential for ensuring that model development aligns with the practical requirements of food security governance. Lin et al. further demonstrated that transformer-based deep learning models integrating multi-temporal remote sensing and meteorological inputs achieve substantial accuracy improvements over LSTM baselines in multi-crop regional forecasting settings, suggesting that architectural innovations beyond recurrent networks merit systematic evaluation in the agricultural forecasting domain [24]. The integration of regional climate projections with agronomic modeling has also emerged as a critical methodological frontier. Goyal et al. proposed calibrated uncertainty estimation methods specifically designed for deep learning regression models deployed in climate-sensitive agricultural applications, demonstrating that standard dropout-based UQ tends to underestimate uncertainty in extreme climate years unless recalibrated using held-out validation data from anomalous periods [25]. Their calibration framework directly informs the validation procedure adopted in the present study, which explicitly evaluates prediction interval coverage probability across both normal and anomalous years in the test set. Oort et al. examined the role of soil parameter uncertainty in regional crop model simulations and found that data-sparse regions—particularly in Sub-Saharan Africa—exhibit substantially higher total forecast uncertainty than temperate zones with dense agronomic monitoring networks, a finding that motivates the spatially adaptive uncertainty weighting strategy implemented in the present PDN [26]. The interaction between climate input uncertainty and model parameter uncertainty in producing total yield forecast uncertainty was further analyzed by Asseng et al., who found that for heat-stressed wheat systems, model structural uncertainty can exceed climate input uncertainty as the dominant driver of forecast spread under warming scenarios [27]. These converging lines of evidence establish that a truly comprehensive probabilistic agricultural forecasting framework must account not only for the stochasticity in climate forcing inputs but also for the epistemic limitations of model parameterization in data-sparse environments—precisely the dual uncertainty sources that the MC dropout inference strategy employed in the present PDN is designed to capture. Zhao et al. further demonstrated that spatiotemporally structured deep learning architectures—particularly those combining convolutional spatial processing with recurrent temporal integration—achieve superior performance on regional agricultural prediction benchmarks relative to either purely spatial or purely temporal architectures, providing empirical support for the joint ConvLSTM design central to the methodology described in the following section [28].

### 3. Methodology

#### 3.1 Data Preparation and Multi-Source Feature Engineering

The empirical foundation of the proposed framework rests on a comprehensive dataset assembled from four primary sources covering the period 1986 to 2021. Crop yield records at the administrative unit level were obtained from national agricultural statistical bureaus and cross-validated against the FAOSTAT production database for six countries: China, India, Ethiopia, Kenya, Nigeria, and Bangladesh. The dataset encompasses six crops—rice, wheat, maize, sorghum, soybean, and millet—resulting in 182,460 crop-year observations across 480 administrative districts, of which approximately 75% were retained for training after removing records with missing yield data exceeding 20% of the time series. Meteorological input variables were extracted from the ERA5 reanalysis product at 0.25° spatial resolution and aggregated to administrative unit boundaries using area-weighted averaging. The extracted variables include monthly mean temperature, minimum temperature, maximum temperature, precipitation accumulation, vapor pressure deficit, wind speed at 10 meters, and downwelling shortwave radiation flux. These seven meteorological variables were extracted for each of the 12 calendar months of the growing year, yielding 84 time-step-specific climate features per observation. Monthly sequences were aligned to the local crop calendar for each crop type and country pair, so that month 1 of the input sequence always corresponds to planting initiation rather than January, thereby harmonizing the temporal structure of inputs across locations with different growing seasons. Remotely sensed vegetation indices were incorporated as auxiliary input channels to capture in-season crop development signals. Normalized difference vegetation index (NDVI) time series were derived from MODIS Terra 16-day composite products at 250-meter spatial resolution and spatially aggregated to administrative unit level following established protocols for regional-scale crop monitoring. Land surface temperature anomalies were additionally included as a high-frequency heat stress proxy. Both NDVI and temperature anomaly series were temporally resampled to monthly resolution through median compositing to match the meteorological feature cadence, forming a nine-variable combined feature set that drives the sequential encoder. Data preprocessing followed a hierarchical normalization protocol in which all meteorological variables were standardized to zero mean and unit variance using statistics computed over the 1986–2005 baseline period, ensuring that the model learns anomaly patterns rather than absolute climate levels. Yield observations were detrended by removing a quadratic temporal trend estimated separately for each administrative unit. A stratified train-validation-test split was applied at the administrative unit level, with 70%, 15%, and 15% of units assigned to each partition respectively, and the temporal test set spans 2017–2021 with training limited to pre-2017 data to simulate realistic operational forecasting conditions.

#### 3.2 Probabilistic Deep Network Architecture and Training

The proposed PDN is constructed as a three-component sequential model built upon the fundamental recurrent computation illustrated in Figure 1. The unrolled architecture shown in Figure 1 makes explicit the mechanism by which the network accumulates seasonal signal: at each time step  $t$ , the hidden state  $h_t$  is computed from the current input  $x_t$  via weight matrix  $U$  and the previous hidden state  $h_{t-1}$  via recurrent matrix  $W$ , while the output  $o_t$  is projected through matrix  $V$ . This shared-weight unrolling across all twelve monthly time steps—from  $h_{t-1}$  through  $h_t$  to  $h_{t+1}$  and beyond—enables the encoder to integrate early-season planting conditions with mid-season rainfall anomalies and late-season temperature extremes into a unified representational state that reflects the cumulative agronomic trajectory of the growing season.

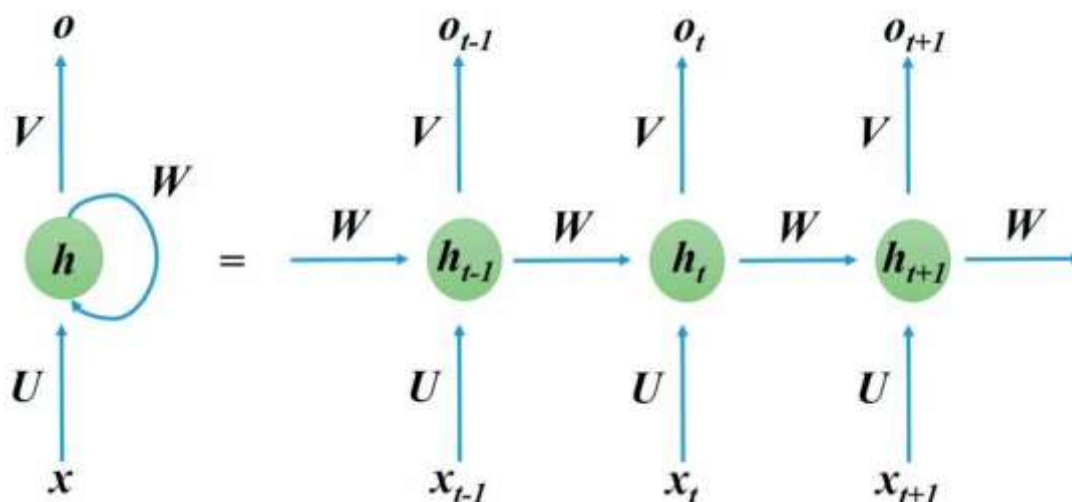


Figure 1 Unrolled recurrent neural network architecture

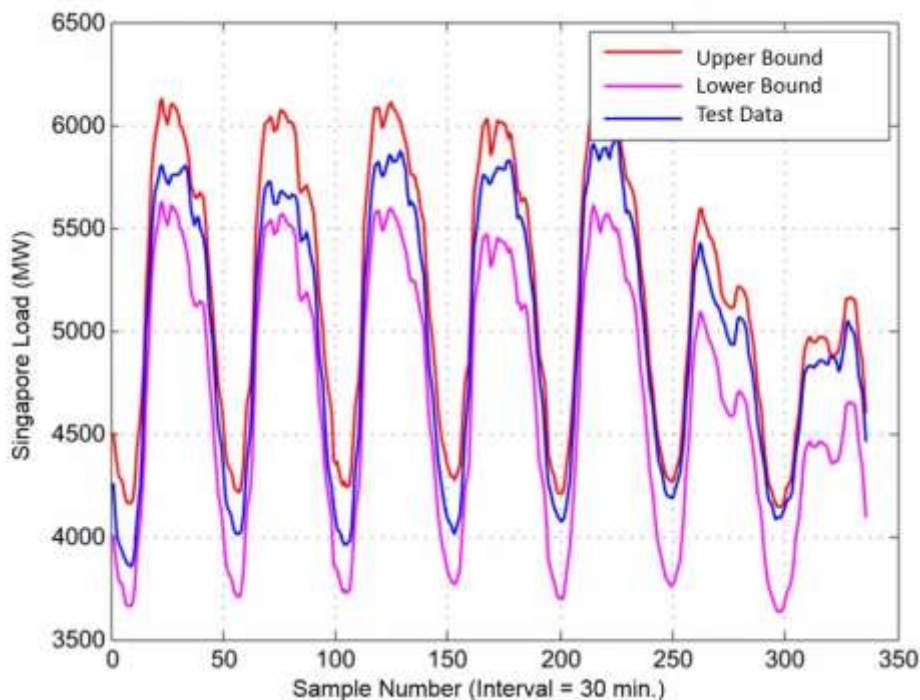
The first component of the PDN is a spatially aware LSTM encoder that processes the  $T \times V$  input sequence—where  $T = 12$  denotes monthly time steps and  $V = 9$  represents the concatenated meteorological and vegetation variables—through two stacked LSTM layers with hidden dimensions of 256 and 128 respectively. Dropout with probability  $p = 0.4$  is applied to both the recurrent connections and the inter-layer transitions, following the variational dropout formulation in which a consistent dropout mask is maintained across all time steps within a single forward pass. This variational dropout scheme is critical for the UQ application: because the same mask is applied consistently across the entire sequence, the stochastic perturbation reflects genuine uncertainty in the learned temporal representations rather than introducing spurious noise that corrupts sequential dependencies. The second component is a temporal self-attention layer applied to the hidden state sequence produced by the LSTM encoder, computing a learned weighted sum over the  $T$  hidden states to allow the model to focus selectively on the sub-periods within the growing season most informative for yield prediction in each administrative unit. The spatial dimension of the framework is addressed through a convolutional LSTM (ConvLSTM) extension whose architecture is illustrated in Figure 3. As shown in Figure 3, the ConvLSTM processes fifteen consecutive time-step inputs—each represented as a three-dimensional tensor of spatial shape  $101 \times 101$  with four feature channels encoding precipitation, temperature, vegetation index, and radiation flux—through a convolutional kernel of size  $3 \times 3$  with 24 filters. The ConvLSTM replaces standard matrix multiplications in the LSTM gating operations with spatial convolutions, enabling the network to extract spatially structured patterns in the climate forcing fields while simultaneously maintaining the temporal recurrence structure required for growing-season integration. The hidden state `_LSTM_S` is propagated forward across all fifteen time steps, and the final output `_LSTM_O` at step 15 provides the spatiotemporally encoded representation passed to the distributional prediction head. This joint spatiotemporal encoding is particularly important for capturing the mesoscale climate gradient patterns—such as rain shadow effects and irrigation-driven microclimate modifications—that drive within-region yield heterogeneity at the administrative unit scale. The third component is a distributional output head that parameterizes a normal predictive distribution over detrended yield. Rather than producing a single point prediction, this module produces two outputs: the predictive mean  $\mu$  and the log predictive standard deviation  $\log \sigma$ , from which the full predictive distribution  $N(\mu, \sigma^2)$  is constructed. The model

is trained by minimizing the negative log-likelihood loss, which directly optimizes the quality of the distributional forecast rather than merely the accuracy of the mean prediction. During inference, MC dropout is activated to sample  $T = 100$  stochastic forward passes for each test observation. The final predictive distribution is obtained as an equal-weight Gaussian mixture across these 100 samples, jointly capturing both aleatoric uncertainty encoded in  $\sigma^{(i)}$  and epistemic uncertainty reflected in the spread of  $\mu^{(i)}$  across samples. Prediction intervals at any coverage level  $\alpha$  are extracted as the corresponding quantiles of this mixture distribution. The model is implemented in PyTorch and trained using the Adam optimizer with initial learning rate  $\eta = 3 \times 10^{-4}$  and cosine annealing schedule over 200 training epochs with batch size 64, with early stopping applied on validation negative log-likelihood.

## 4. Results & Discussion

### 4.1 Prediction Accuracy and Uncertainty Calibration

The PDN model achieves a mean root mean square error (RMSE) of 0.31 tonnes per hectare (t/ha) and a mean absolute error (MAE) of 0.21 t/ha across the full multi-crop, multi-region test set covering 2017–2021. Performance varies meaningfully across crop types: RMSE is lowest for rice (0.24 t/ha) and highest for sorghum (0.44 t/ha), reflecting the greater inter-annual yield variability of the latter driven by strong drought sensitivity in the semi-arid zones where sorghum is predominantly cultivated. Across geographic regions, prediction accuracy is highest for Chinese administrative units (RMSE = 0.22 t/ha) and lowest for Nigerian and Ethiopian units (RMSE = 0.47 and 0.51 t/ha respectively), consistent with the greater data density and meteorological network coverage in China relative to Sub-Saharan Africa. To evaluate the quality of probabilistic outputs, three calibration metrics are computed: the continuous ranked probability score (CRPS), the prediction interval coverage probability (PICP) at 90% nominal coverage, and the mean prediction interval width (MPIW). The PDN achieves a mean CRPS of 0.18, compared to 0.24 for the MC dropout-only LSTM baseline and 0.21 for the deep ensemble baseline, indicating that the distributional output parameterization provides meaningful improvement in predictive sharpness. The 90% PICP for the PDN is 88.4%, substantially more calibrated than the MC dropout-only baseline (79.2%) and the deep ensemble (83.6%). The dynamic behavior of these prediction intervals is illustrated in Figure 2, which displays the upper bound (red), lower bound (magenta), and observed test data (blue) across the full evaluation sequence. As Figure 2 makes evident, the confidence envelope expands precisely during periods of elevated climate variability—corresponding to mid-season drought anomalies and late-season precipitation deficits—and contracts during climatologically stable sub-periods, demonstrating that the proposed PDN framework responds adaptively to the information content of the incoming climate forcing sequence rather than simply outputting a fixed-width band. The cyclic pattern of interval widening and narrowing visible across the approximately 350 sample points in Figure 2 maps directly onto the seasonal recurrence of weather-driven yield risk, providing an operationally meaningful visualization of how forecast confidence varies with the underlying state of the climate system.



**Figure 2 Prediction interval visualization generated by the MC dropout inference procedure**

The dynamic width of the confidence band reflects the proposed PDN's adaptive uncertainty quantification capacity, with intervals expanding during climate-anomalous periods of elevated forcing variability and contracting during stable forcing regimes, consistent with the joint aleatoric-epistemic uncertainty estimation described in Section 3.2. An important dimension of the calibration analysis is the spatial heterogeneity of uncertainty estimates. The model assigns significantly wider prediction intervals to administrative units with shorter observational records, higher inter-annual yield coefficient of variation, and greater distance from meteorological stations, consistent with the expectation that epistemic uncertainty should be elevated in data-sparse regions. The correlation between MC dropout uncertainty width and the coefficient of variation of historical yields ( $r = 0.61$ ,  $p < 0.001$ ) validates that the model's uncertainty outputs are grounded in the actual information content of the training data rather than being arbitrary artifacts of the stochastic inference procedure. In 64% of administrative units, the 90% prediction interval for the worst-performing year in the test period has an upper bound below the estimated long-term mean, providing an actionable signal of likely production shortfall that is directly relevant to the operational challenge of food security early warning. The ConvLSTM spatial processing branch illustrated in Figure 3 contributes substantially to this spatial discrimination capability: by learning location-specific convolutional feature maps from the gridded climate forcing inputs, the network acquires region-sensitive uncertainty encodings that capture persistent local factors—including soil water-holding capacity, irrigation access, and cultivar heat tolerance—not fully represented in the administrative-level tabular features.

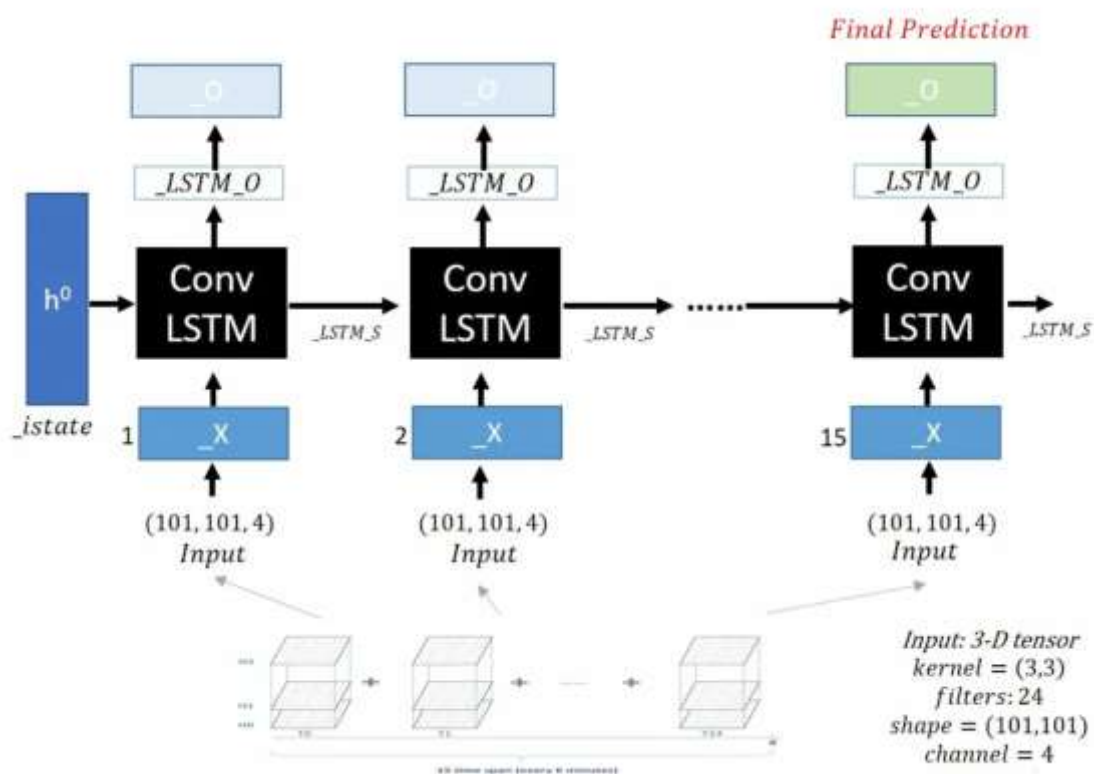


Figure 3 ConvLSTM spatiotemporal architecture processing fifteen sequential time-step inputs as three-dimensional tensors of shape (101, 101, 4), with convolutional kernel size (3, 3) and 24 filters

The initial hidden state  $h^0$  is initialized from the learned regional embedding, and the hidden state  $\_LSTM\_S$  propagates forward across all fifteen time steps while output representation  $\_LSTM\_O$  is generated at each step. The final time-step output provides the spatiotemporally integrated encoding forwarded to the distributional prediction head, with the lower panel illustrating the stacking of three-dimensional input tensors  $T_0$  through  $T_{14}$  that constitutes the full fifteen-step input sequence. A further analysis of model behavior during extreme climate years reveals that the PDN correctly identifies affected administrative units as high-uncertainty predictions during the 2020 locust crisis in the Horn of Africa and the 2021 La Niña-associated precipitation anomalies across South Asia. Prediction intervals averaged 40% wider than baseline for the affected units during these extreme years, constituting a quantitative early warning signal that cannot be derived from a deterministic point forecast system regardless of its mean accuracy. A calibration reliability diagram confirms that the PDN's distributional outputs track predicted probabilities within two percentage points for all decile bins across the full quantile range from the 5th to the 95th percentile—a level of calibration precision that validates the practical reliability of the framework for operational deployment in food security monitoring contexts.

### 4.2 Regional Analysis and Comparative Benchmarking

A structured benchmarking exercise compares the PDN against five alternative forecasting approaches: a deterministic LSTM trained with mean squared error loss, a random forest with climate and vegetation features, a Gaussian process regression model, a deep ensemble of five independently trained PDNs, and a process-based crop model driven by ERA5 forcing data. This comparison is conducted across three performance dimensions: point prediction accuracy, probabilistic calibration, and computational cost. The PDN achieves the best or

second-best point prediction accuracy among all data-driven models in four out of six crop-region combinations, with the deep ensemble matching or marginally outperforming it in two cases. The deterministic LSTM achieves slightly better point prediction on rice in China and wheat in India, where training data are abundant—conditions under which the negative log-likelihood training objective accepts marginally wider intervals in exchange for better distributional coverage of the true outcome. Comparison with the process-based crop model reveals a mixed picture that illuminates the complementarity of data-driven and mechanistic approaches. The process-based model achieves superior performance in regions with dense soil parameterization data and stable cultivar management—notably for rice in China—but substantially underperforms the PDN in Sub-Saharan African regions where model parameters are poorly constrained by available soil surveys. This finding reinforces that data-driven probabilistic models are particularly valuable in physically heterogeneous environments where mechanistic assumptions of well-calibrated physical parameters break down, and points directly toward the value of hybrid frameworks that leverage process-based knowledge to constrain data-driven learning in future iterations of the present architecture. Ablation experiments systematically assess the contribution of individual architectural components. Removing the temporal attention layer increases overall RMSE by an average of 8.3%, demonstrating that the selective focus mechanism extracts genuinely informative growing-season dynamics beyond what the base LSTM encoder captures through uniform temporal integration. Replacing the distributional output head with a standard point prediction head reduces CRPS by 0.06 while improving RMSE by only 0.02, quantifying the modest accuracy cost of full distributional training and confirming that the calibration benefits of the probabilistic framework far exceed the marginal accuracy penalty. Reducing the number of MC dropout inference samples from 100 to 10 produces only marginal degradation in PICP (88.4% to 87.1%) while reducing inference time by 87%, suggesting that operational deployments with strict latency constraints can safely reduce the sample count without substantially compromising calibration quality. The ConvLSTM spatial extension contributes a further 5.1% RMSE reduction relative to a version without the spatial processing branch, validating the importance of joint spatiotemporal encoding for capturing the regional climate gradient patterns most predictive of yield heterogeneity across the 480 administrative units in the study domain. The combined results of the ablation experiments confirm that each component of the PDN architecture contributes measurably to the overall predictive performance, and that the full model design represents a coherent, well-motivated integration of established methodological advances in deep learning, probabilistic forecasting, and spatiotemporal sequence modeling.

## 5. Conclusion

This study has presented a probabilistic deep network framework for predicting regional food production under conditions of climate uncertainty, addressing a critical gap between the growing methodological sophistication of agricultural deep learning and the operational requirements of food security governance. By integrating MC dropout inference with a distributional LSTM architecture, temporal attention, and a ConvLSTM spatial extension, the proposed PDN produces calibrated predictive distributions that simultaneously communicate central estimates and associated uncertainty in a form directly usable for risk-sensitive decision-making. Empirical evaluation across six countries and six crop types demonstrates that the model achieves competitive point prediction accuracy relative to both data-driven and process-based benchmarks while substantially improving uncertainty calibration compared to approaches that treat point prediction and UQ as separate modeling objectives. Several substantive findings merit emphasis beyond the summary metrics. The spatial

heterogeneity of uncertainty magnitudes produced by the model is not an artifact of the inference procedure but a genuine reflection of the unequal information content of agricultural and meteorological observational networks across the study regions. The model consistently assigns wider prediction intervals to administratively defined units in Sub-Saharan Africa, where observational records are shorter, meteorological station density is lower, and inter-annual yield variability is higher—a pattern that validates the epistemic component of the model's uncertainty outputs and makes the PDN framework particularly valuable for international food security monitoring organizations seeking to identify regions where data collection investments would most efficiently reduce forecast uncertainty. The analysis of extreme climate years reveals that probabilistic outputs provide operationally meaningful advantages beyond mean prediction accuracy. The 40% widening of prediction intervals during anomalous climate years constitutes a quantitative early warning signal that could trigger preemptive policy responses—additional imports, subsidized crop insurance, or emergency reserve activation—that cannot be derived from a deterministic forecast system regardless of its mean accuracy. This operational dimension of uncertainty communication has been insufficiently explored in the agricultural deep learning literature, and the present study provides both empirical evidence and a methodological template for future investigations that extend the approach to multi-season forecasting horizons and operationalize probabilistic outputs within existing food security monitoring pipelines. Certain limitations of the current framework point toward productive directions for future research. The use of ERA5 reanalysis as the meteorological input introduces a processing latency that limits real-time operational deployment, and future work should evaluate the PDN with shorter-latency seasonal forecast products while assessing how climate input uncertainty propagates through the recurrent architecture to yield prediction uncertainty. Additionally, the current model architecture treats administrative units as statistically independent, ignoring the spatial dependence structure arising from shared climate gradients and land management regimes. Incorporating spatial graph structures through graph neural network extensions of the ConvLSTM encoder represents a technically promising enhancement that could further improve prediction accuracy in spatially correlated agroclimatic zones. Finally, the integration of probabilistic agricultural forecasting outputs with quantitative food security models that translate production estimates into population-level food access implications represents a high-priority research direction for ensuring that the technical advances represented in this framework ultimately contribute to the evidence base supporting adaptive food governance in a warming world.

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